

# STA 570 — Spring 2012 — Dr. Charnigo

## Written Assignment 6

This assignment is due on Thursday 26 April at 12 Noon. You may work in self-selected groups of two or three, submitting one copy of the assignment for the group.

[60] 1. The data set {BirthWeight.xls} provides gestational ages (in weeks) and birth weights (in grams) for 700 infants. Let  $X$  denote gestational age and  $Y$  birth weight. Consider a linear regression model of the form

$$Y_i = \alpha + \beta x_i + \epsilon_i.$$

You may proceed as if the  $\epsilon_i$  were independent normal random variables with mean 0 and unknown but common variance  $\sigma^2$ .

[10] a. Report the least squares estimates of  $\alpha$  and  $\beta$ .

[10] b. Report 95% confidence intervals for  $\alpha$  and  $\beta$ .

[10] c. Test  $H_0 : \beta = 0$  by constructing an ANOVA table and calculating an  $f$  statistic.

[10] d. Test  $H_0 : \beta = 0$  by calculating a  $t$  statistic based on the least squares estimate of  $\beta$ .

[10] e. Calculate  $R^2$  and describe in words what  $R^2$  represents in this exercise.

[10] f. Provide a 95% confidence interval for the mean birth weight among all infants with gestational age 37 weeks.

[40] 2. Let  $p_1$  and  $p_2$  be as defined in exercise 1 of Written Assignment 4.

[10] a. Report point and 95% interval estimates for the risk difference  $p_1 - p_2$ .

[10] b. Report point and 95% interval estimates for the relative risk  $p_1/p_2$ .

[10] c. Report point and 95% interval estimates for the odds ratio  $\{p_1/(1 - p_1)\}/\{p_2/(1 - p_2)\}$ .

[10] d. How do your 95% interval estimates relate to the outcomes of the hypothesis tests conducted in exercise 1 of Written Assignment 4 ?